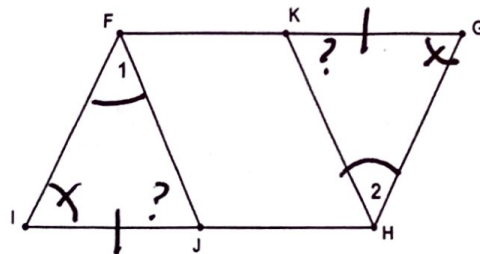


Unit 5 Day 1 Warmup

1. Given:  $\angle I \cong \angle G$   
 $\angle 1 \cong \angle 2$   
 $\overline{JI} \cong \overline{KG}$

Prove:  $\angle HKG \cong \angle FJI$



Given  $\angle I \cong \angle G$       Given  $\angle 1 \cong \angle 2$       Given  $\overline{JI} \cong \overline{KG}$

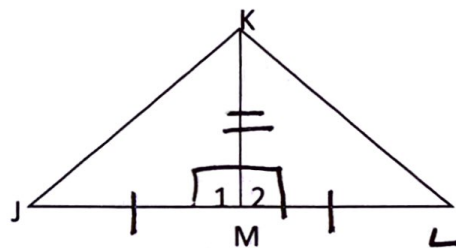
AAS

$\triangle IFJ \cong \triangle GKH$

CPCTC

$\angle HKG \cong \angle FJI$

2. Given:  $\overline{KM} \perp \overline{JL}$   
 $M$  is the midpoint of  $\overline{JL}$   
 Prove:  $\triangle JKM \cong \triangle LKM$



Given  $\overline{KM} \perp \overline{JL}$

Given  $M$  midpt.  $\overline{JL}$

Reflexive Prop.  
 $\overline{KM} \cong \overline{KM}$

Defn  $\perp$  lines  
 $\perp$  lines  $\rightarrow$  right  $\angle$ s

$\angle 1, \angle 2$  are right  $\angle$ s

Defn of midpoint

$\overline{JM} \cong \overline{ML}$

all right  $\angle$ s  $\cong$

$\angle 1 \cong \angle 2$

SAS

$\triangle JKM \cong \triangle LKM$

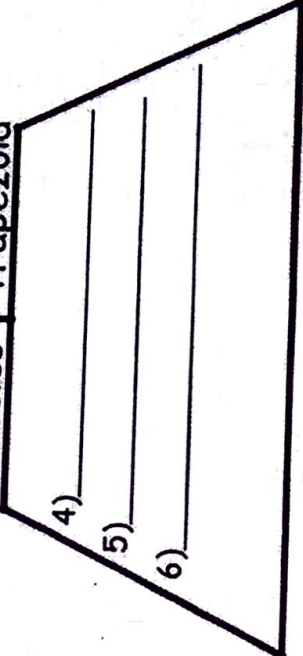
# Properties of Quadrilaterals

Trapezoid

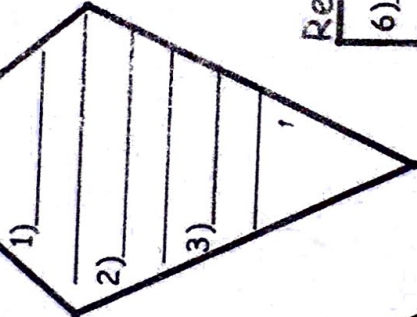


Isosceles

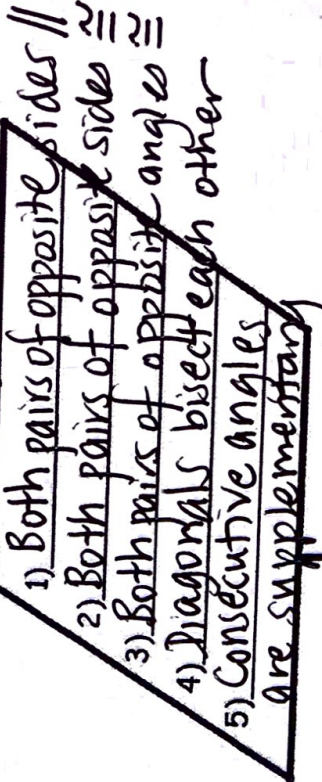
Trapezoid



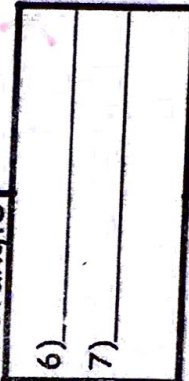
Kite



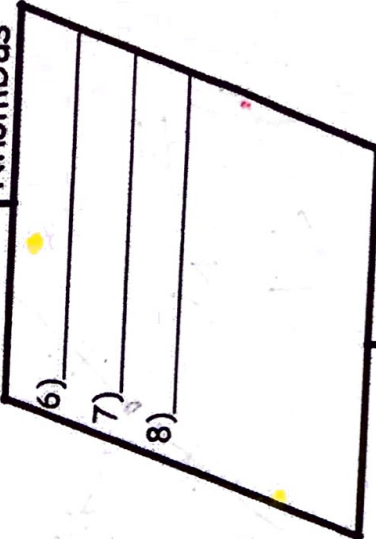
Parallelogram



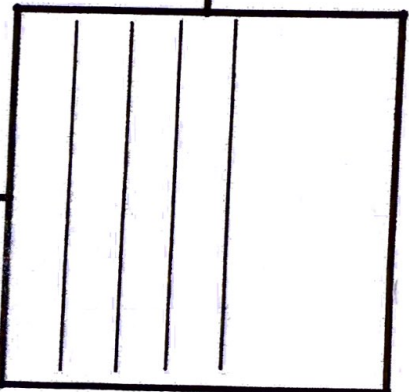
Rectangle



Rhombus



Square

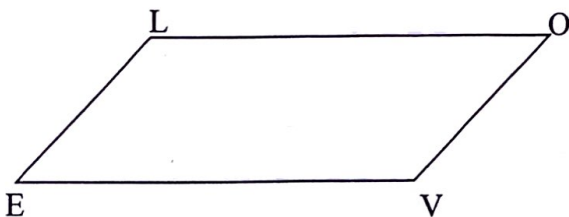


Honors Math 3 - Unit 5 Day 1  
Parallelograms

Define:

QUADRILATERAL - 4-sided polygon

PARALLELOGRAM - a quadrilateral with both pairs of opposite sides parallel.



Using parallelogram LOVE:

The side opposite  $\overline{LO} = \overline{VE}$

The side opposite  $\overline{VO} = \overline{LE}$

The angle opposite  $\angle O = \angle E$

Name a consecutive angle for  $\angle L = \angle O$  or  $\angle E$

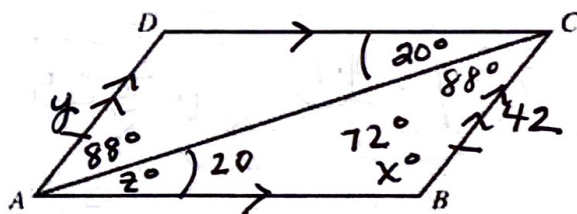
Parallelogram examples:

#1: For the parallelogram, find the values of  $x$ ,  $y$  and  $z$ .

$$y = 42$$

$$z = 20^\circ$$

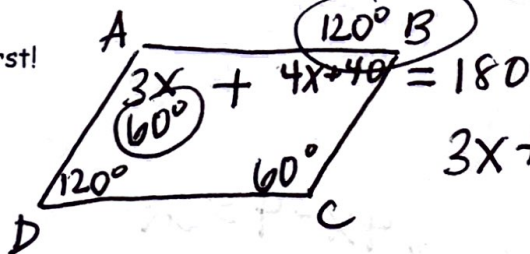
$$x = 72^\circ$$



#2:

In parallelogram ABCD,  $m\angle A = 3x$  and  $m\angle B = 4x + 40$ . Find the measure of angles A, B, C, D.

Draw a parallelogram and label it first!

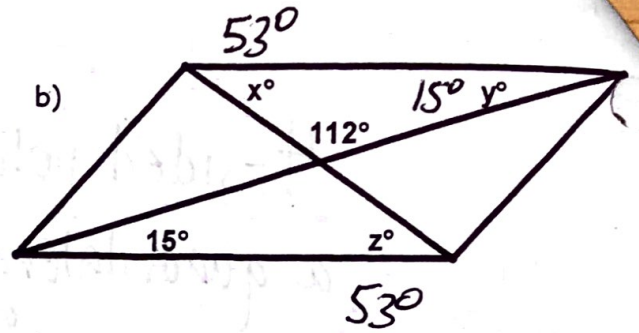
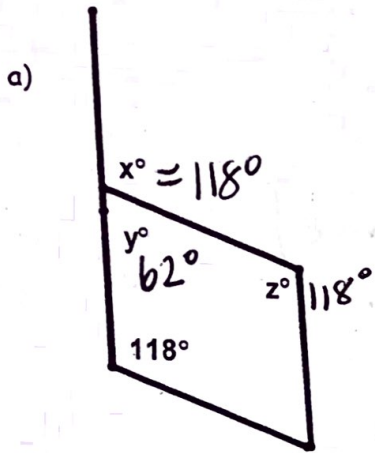


$$3x + 4x + 40 = 180$$

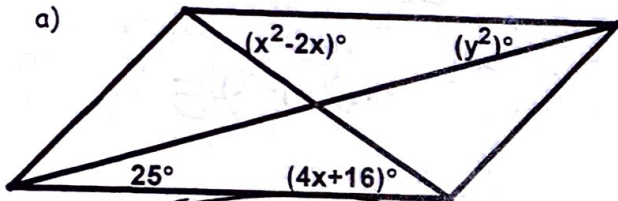
$$7x = 140$$

$$x = 20$$

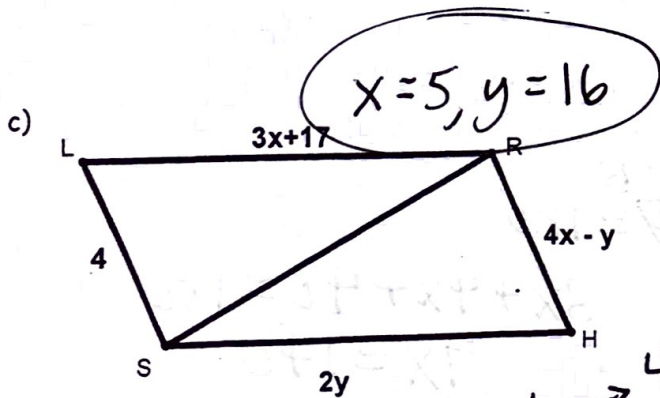
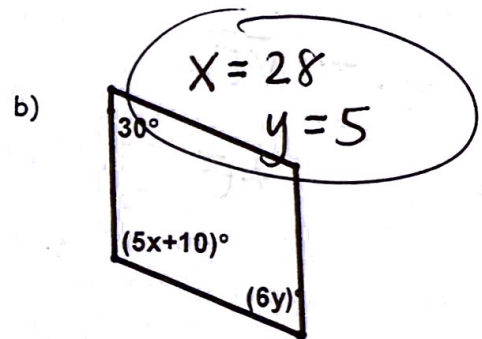
#3 For the parallelograms, find the values of x, y and z.



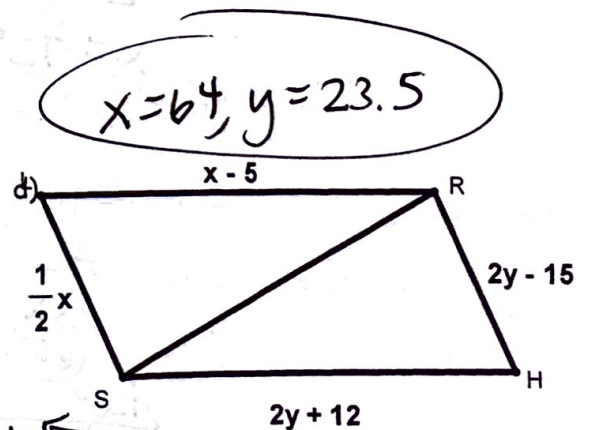
#4 Given the parallelograms, solve for x and y.



$x = 8, -2$   
 $y = \pm 5$   $\sqrt{y^2} = \sqrt{25}$



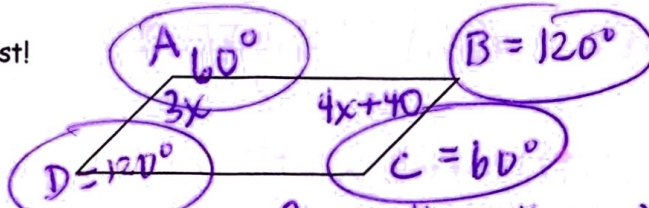
$4x - y = 4 \rightarrow 4x - 4 = y$   
 $3x + 17 = 2y \rightarrow 3x + 17 = 2(4x - 4)$   
 $x = 5$



#2:

In parallelogram ABCD,  $m\angle A = 3x$  and  $m\angle B = 4x + 40$ . Find the measure of angles A, B, C, D.

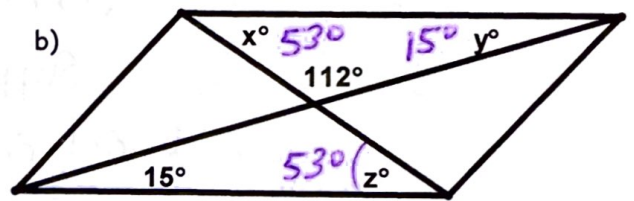
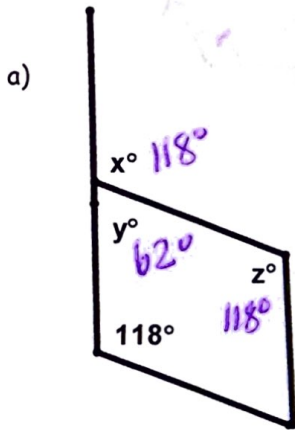
Draw a parallelogram and label it first!



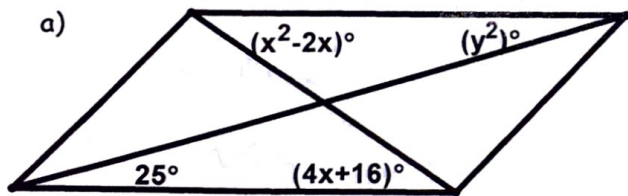
$\angle A$  and  $\angle B$  are supplementary angles, so they are consecutive  $3x + 4x + 40 = 180$   
 $7x + 40 = 180$

$7x = 140$   
 $x = 20$

#3 For the parallelograms, find the values of x, y and z.



#4 Given the parallelograms, solve for x and y.



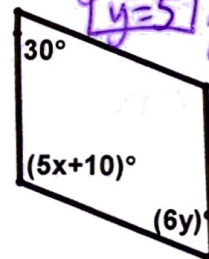
$y^2 = 25$   
 $y = \pm 5$

$x^2 - 2x = 4x + 16$   
 $x^2 - 2x - 4x - 16 = 0$   
 $x^2 - 6x - 16 = 0$   
 $(x+2)(x-8) = 0$   
 $x = -2, 8$

$x = -2, 8$

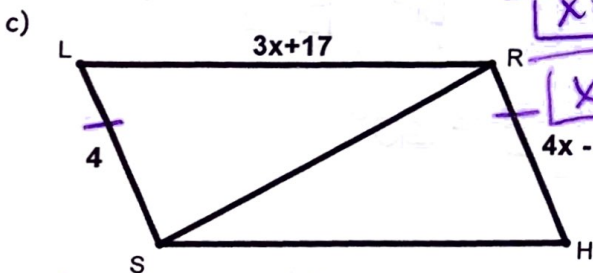
$x = 5$   
 $y = 16$

$6y = 30$   
 $y = 5$   
 $5x + 10 + 30 = 180$   
 $5x + 40 = 180$



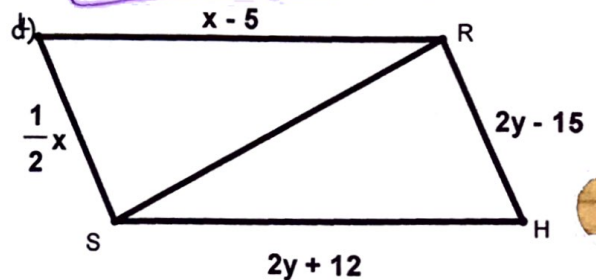
$5x = 140$   
 $x = 28$

$x = 64$   
 $y = 23.5$



$-2(4x - y = 4)$   
 $3x - 2y = -17$

$3x + 17 = 2y$   
 $-8x + 2y = -8$   
 $+ 3x - 2y = -17$   
 $-5x = -25$   
 $x = 5$

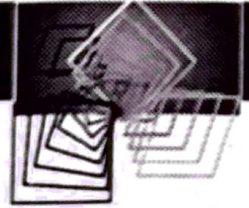


# Quadrilaterals

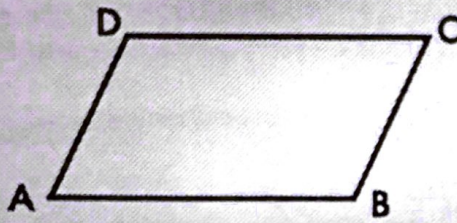


Keep in mind...

If you put forth  $\frac{1}{2}$  the effort, you only get a fraction of the results.



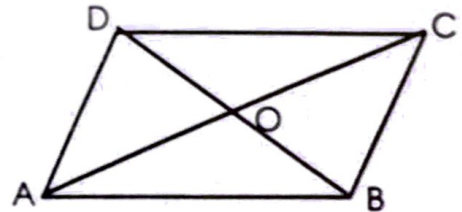
## Properties of Parallelograms



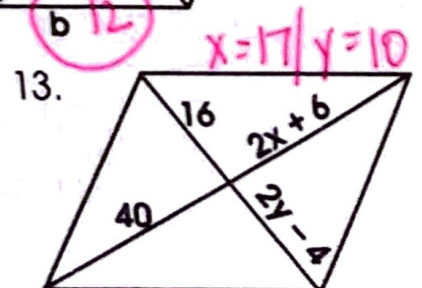
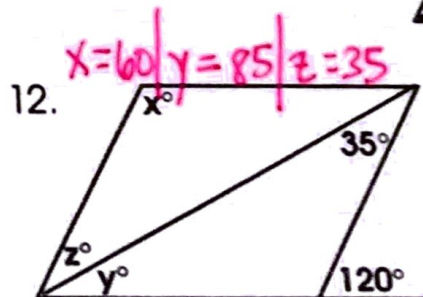
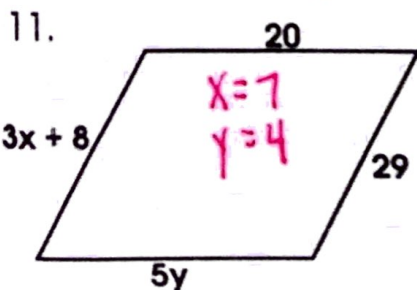
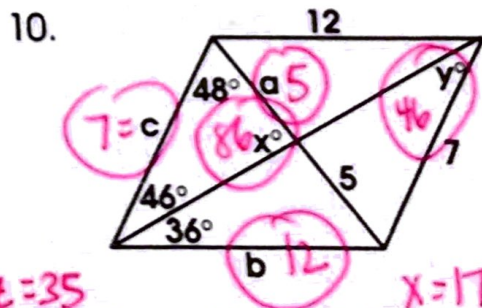
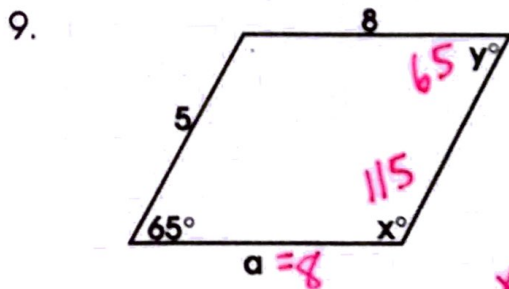
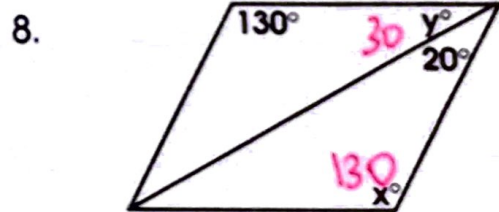
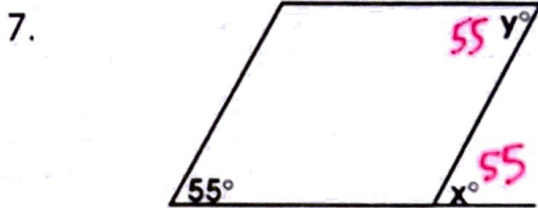
- Four sides.
- Both pair of opposite sides are parallel.
- Both pair of opposite sides are congruent.
- Both pair of opposite angles are congruent.
- Diagonals bisect each other.

Complete the following  $\square ABCD$ .

- |  |  |
|--|--|
| 1. $\overline{AB} \parallel \underline{\overline{DC}}$ | 2. $\overline{AB} \cong \underline{\overline{DC}}$ |
| 3. $\angle A \cong \underline{\angle C}$               | 4. $\overline{OA} \cong \underline{\overline{OC}}$ |
| 5. $\overline{OB} \cong \underline{\overline{OD}}$     | 6. $\overline{AD} \cong \underline{\overline{BC}}$ |



Find the missing values for each parallelogram.

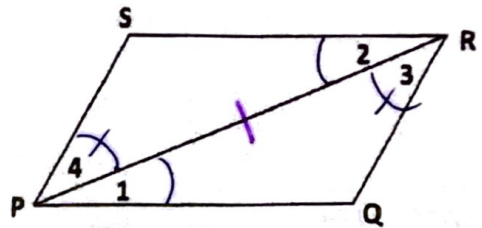


Name: \_\_\_\_\_

Date: \_\_\_\_\_ Period: \_\_\_\_\_

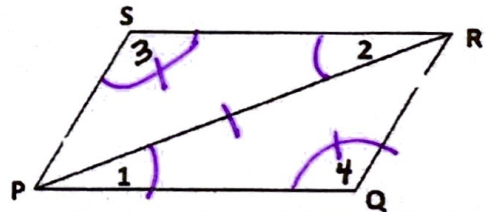
Quadrilaterals Jumble Proofs

1. Given:  $\angle 1 \cong \angle 2$   
 $\angle 3 \cong \angle 4$   
 Prove: PQRS is a parallelogram



Statements	Reasons
① $\angle 1 \cong \angle 2$ $\angle 3 \cong \angle 4$	① Given
② $\overline{PR} \cong \overline{PR}$	② Reflexive Property of $\cong$
③ $\triangle PSR \cong \triangle RQP$	③ Angle-Side-Angle (ASA)
④ $\overline{PS} \cong \overline{RQ}, \overline{SR} \cong \overline{QP}$	④ CPCTC
⑤ PQRS is parallelogram	⑤ if both pairs of opp. sides of quad. $\cong$ , then it is a parallelogram

2. Given:  $\angle 1 \cong \angle 2$   
 $\angle 3 \cong \angle 4$   
 Prove: PQRS is a parallelogram



Statements	Reasons
① $\angle 1 \cong \angle 2, \angle 3 \cong \angle 4$	① Given
② $\overline{PR} \cong \overline{PR}$	② Reflexive Prop. of $\cong$
③ $\triangle PSR \cong \triangle RQP$	③ AAS
④ $\overline{PS} \cong \overline{RQ}, \overline{SR} \cong \overline{QP}$	④ CPCTC
⑤ PQRS is parallelogram	⑤ if both pairs of opp. sides of quad. $\cong$ , then it is a parallelogram.