

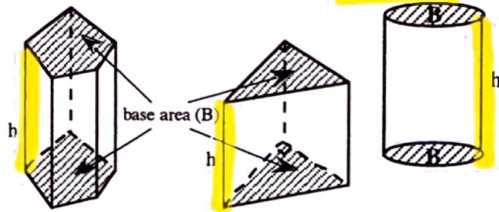
## VOLUME AND SURFACE AREA OF POLYHEDRA

#17

The **VOLUME** of various polyhedra, that is, the number of cubic units needed to fill each one, is found by using the formulas below.

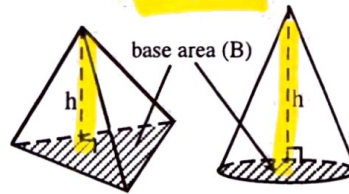
for prisms and cylinders

$$V = \text{base area} \times \text{height}, V = Bh$$



for pyramids and cones

$$V = \frac{1}{3} Bh$$

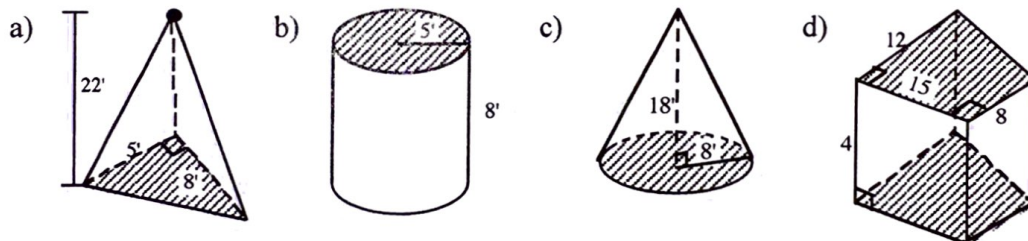


In prisms and cylinders, you may use either base, since they are congruent. Since the bases of cylinders and cones are circles, their area formulas may be expressed as: cylinder  $V = \pi r^2 h$  and cone  $V = \frac{1}{3} \pi r^2 h$

The **SURFACE AREA** of a polyhedron is the sum of the areas of its base(s) and faces.

### Example 1

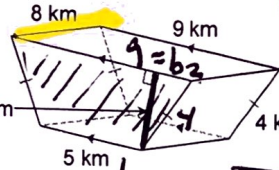
Use the appropriate formula(s) to find the volume of each figure below:



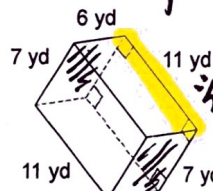
- a) This is a triangular pyramid. The base is a right triangle so the area of the base is  $B = \frac{1}{2} \cdot 8 \cdot 5 = 20$  square units, so  $V = \frac{1}{3} (20)(22) \approx 146.7$  cubic feet.
- b) This is a cylinder. The base is a circle, so  $B = \pi 5^2$ ,  $V = (25\pi)(8) = 200\pi \approx 628.32$  cubic feet.
- c) This is a cone. The base is a circle, so  $B = \pi 8^2$ .  $V = \frac{1}{3} (64\pi)(18) = \frac{1}{3} (64)(18)\pi \Rightarrow = \frac{1}{3} (1152)\pi = 384\pi \approx 1206.37$  feet<sup>3</sup>
- d) This prism has a trapezoidal base, so  $B = \frac{1}{2} (12 + 8)(15) = 150$ . Thus,  $V = (150)(14) = 2100$  cubic feet.

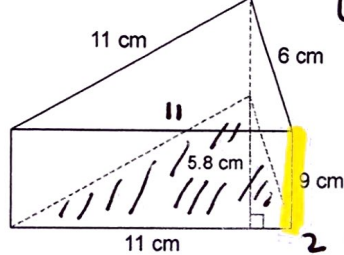
Surface Area P.30  $A_{TRAP} = \frac{1}{2} (b_1 + b_2) h$

Find the surface area of each figure. Round your answers to the nearest hundredth, if necessary. Leave your answers in terms of  $\pi$  for answers that contain  $\pi$ .

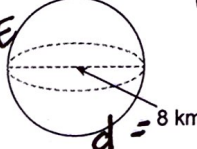
1)  $2B + Ph$   
 $h_B = 3.5$  km  


trapezoidal prism  
 $B = \frac{1}{2} (5+8) 3.5$   
 $B = 24.5$   
 $P = 5+4+9+4 = 22$   
 $S = 2(24.5) + 22(8)$   
 $S = 225 \text{ Km}^2$

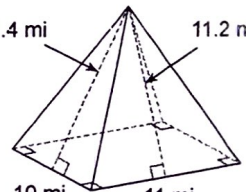
2) rect. prism  $\rightarrow S = 2B + Ph$   
 $B = 6(7) = 42$   
 $P = 2(6) + 2(7) = 26$   
  
 $S = 2(42) + (26)(11)$   
 $S = 370 \text{ yd}^2$

3)  $\Delta$  prism  


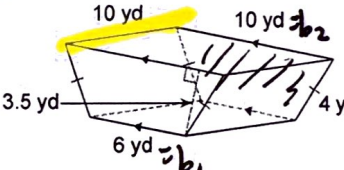
SPHERE  
 $B = \frac{1}{2} (11)(5.8)$   
 $B = 31.9$   
 $P = 11+11+6 = 28$   
 $S = 2(31.9) + 28(9)$   
 $S = 315.8 \text{ cm}^2$

4) SPHERE  
  
 $d = 8 \text{ km}$   
 $r = 4$

$S = 4\pi(4)^2$   
 $S = 201.06 \text{ Km}^2$


5) 

$B = \frac{1}{2} (6+10)(3.5) = 28$   
 $P = 4+4+6+10 = 24$   
 $S = 2(28) + 24(10)$   
 $S = 296 \text{ yd}^2$

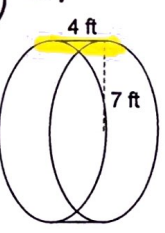
6) PRISM  


$B = \frac{1}{2} (6+10)(3.5) = 28$   
 $P = 4+4+6+10 = 24$

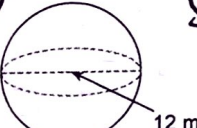
$S = 2(28) + 24(10)$   
 $S = 296 \text{ yd}^2$

7) CONE!  
  
 $11 \text{ km} = r$   
 $s = 24.6 \text{ km}$

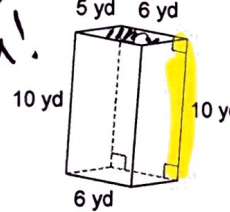
8) CYLINDER  
 $S = \pi(11)^2 + \pi(11)(24.6)$   
 $S = 1230.25 \text{ km}^2$   
 $h^2 + r^2 = s^2$

8) CYLINDER  
  
 $4 \text{ ft}$   
 $7 \text{ ft}$

$S = 2\pi(4)(7+4)$   
 $S = 483.81 \text{ ft}^2$

9)   
 $12 \text{ m}$

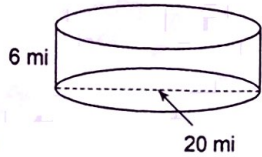
$S = 4\pi(12)^2$   
 $S = 452.39 \text{ m}^2$

10) PRISM!  
  
 $5 \text{ yd}$   
 $6 \text{ yd}$   
 $10 \text{ yd}$

$B = 5 \cdot 6 = 30$   
 $P = 2(5) + 2(6) = 10 + 12 = 22$

$S = 2(30) + 22(10)$   
 $S = 280 \text{ yd}^2$

11)



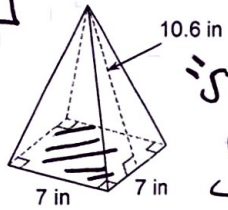
p.31

Square Pyramid

$$B = 7 \cdot 7 = 49$$

$$P = 7(4) = 28$$

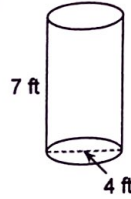
13)



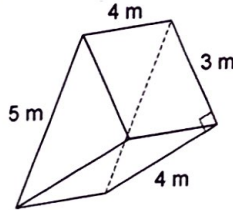
$$S = 49 + \frac{1}{2}(28)(10.6)$$

$$= 197.4 \text{ in}^2$$

12)



14)



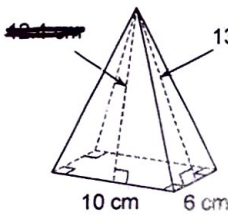
$$B = \frac{1}{2}(4)(3)$$

$$= 10.75$$

$$P = 5(3) = 15$$

15)

rect. pyr.

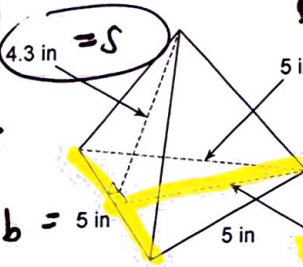


$$B = 10(6) = 60$$

$$P = 2(10) + 2(6) = 32$$

Pyramid

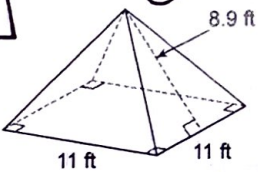
16)



$$S = 10.75 + \frac{1}{2}(15)(4.3)$$

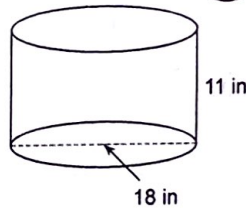
$$= 43 \text{ in}^2$$

17)

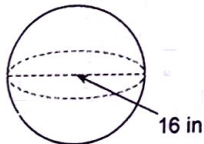


$$S = 60 + \frac{1}{2}(32)(13) = 268 \text{ cm}^2$$

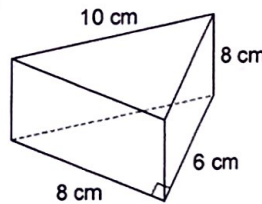
18)



19)



20)





Volume

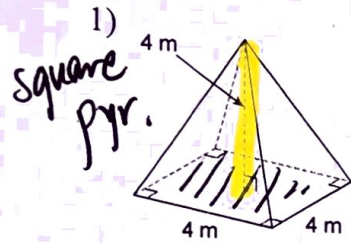
P.34

PRISM/CYL. }  
 $V = Bh$

PYRAMID/CONE

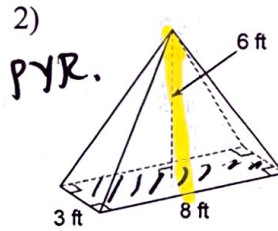
$V = \frac{1}{3} Bh$

Find the volume of each figure. Round your answers to the nearest hundredth, if necessary.



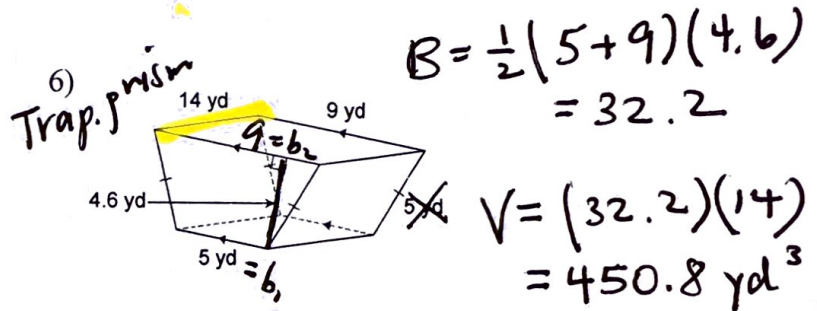
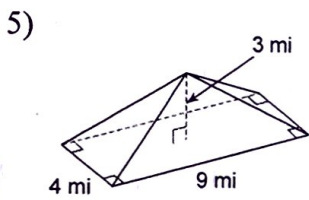
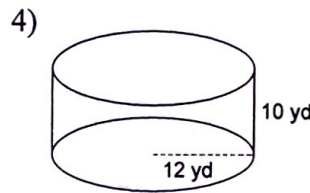
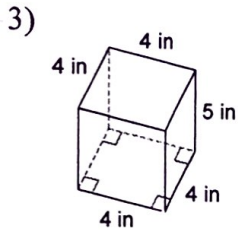
$B = 4 \cdot 4 = 16$

$V = \frac{1}{3} (16)(4)$   
 $= 21.33 \text{ m}^3$



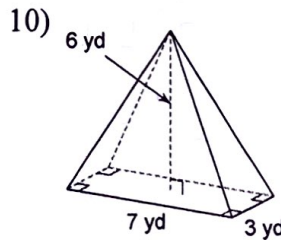
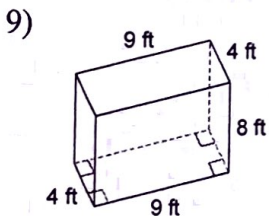
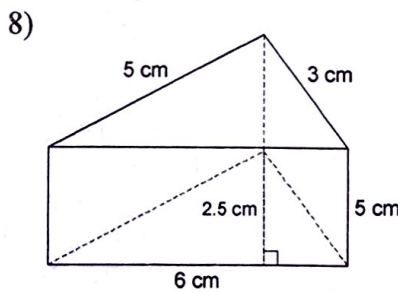
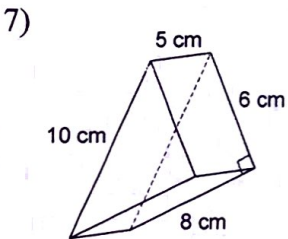
$B = 3 \cdot 8 = 24$

$V = \frac{1}{3} (24)(6)$   
 $= 48 \text{ ft}^3$



$B = \frac{1}{2} (5+14)(4.6)$   
 $= 32.2$

$V = (32.2)(9)$   
 $= 289.8 \text{ yd}^3$



HW:  
 V P.34,35  
 P.31-SA