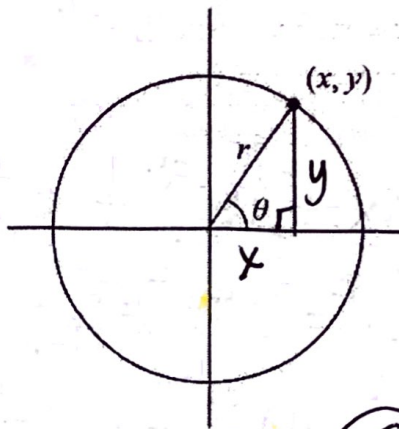


Equations of Circles Guided Notes

Name: _____

Equation of a Circle Centered at the Origin:

$$x^2 + y^2 = r^2$$



What if the center is not at the origin?
How do we transform graphs?

Equation of a Circle Centered at (h, k)

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(2\sqrt{3})^2 = 4 \cdot 3 = 12$$

This is what we call standard form for an equation of a circle.

$$r = 2\sqrt{3} \quad C(-3, 2)$$

$$(x+3)^2 + (y-2)^2 = 12$$

Write an equation of a circle with:

1. radius = 8, center = $(4, 3)$.

$$(x-4)^2 + (y-3)^2 = 64$$

2. radius = 7, center = $(-3, -8)$.

$$(x+3)^2 + (y+8)^2 = 49$$

Find the center and radius a circle with the equation of:

3. $(x-1)^2 + (y+4)^2 = 81$.

$$C(1, -4) \quad r = \sqrt{81} = 9$$

4. $(x-2)^2 + (y+3)^2 = 9$.

$$C(2, -3) \quad r = 3$$

5. Expand the binomial expressions in problem #4, simplify, and set the equation equal to 0.

This is called the general (or expanded) form of the equation of a circle.

From General Form to Standard Form $(x-h)^2 + (y-k)^2 = r^2$

To get an equation of a circle from general form to standard form, you must complete the square.

1. Given $x^2 - 8x + y^2 + 11 = 0$, put in standard form.

$(x-4)(x-4) \swarrow$

$$(x^2 - 8x + \underline{16}) + y^2 = -11 + \underline{16}$$

$$\left(\frac{-8}{2}\right)^2 = (-4)^2 = 16$$

$$\boxed{(x-4)^2 + y^2 = 5}$$

STANDARD FORM

$C(4, 0)$
 $r = \sqrt{5}$

2. Given $x^2 + y^2 + 4x - 6y = -4$, put in standard form.

$$(x^2 + 4x + \underline{4}) + (y^2 - 6y + \underline{9}) = -4 + \underline{4} + \underline{9}$$

$$\left(\frac{4}{2}\right)^2 = (2)^2 = 4 \quad \left(\frac{-6}{2}\right)^2 = (-3)^2 = 9$$

$$\boxed{(x+2)^2 + (y-3)^2 = 9}$$

$C(-2, 3)$
 $r = 3$

3. Given $3x^2 - 9 - 3y^2 - 6y = 0$, put in standard form.

$$x^2 + y^2 + 10x + 4y - 92 = 0$$

$$(x^2 + 10x + \underline{25}) + (y^2 + 4y + \underline{4}) = 92 + \underline{25} + \underline{4}$$

$$\boxed{(x+5)^2 + (y+2)^2 = 121}$$

$C(-5, -2)$
 $r = 11$

4) $x^2 + y^2 - 18x + 16y + 109 = 0$

$$(x^2 - 18x + \underline{81}) + (y^2 + 16y + \underline{64}) = -109 + \underline{81} + \underline{64}$$

$$\left(\frac{-18}{2}\right)^2 = (-9)^2 = 81 \quad \left(\frac{16}{2}\right)^2 = (8)^2 = 64$$

$$\boxed{(x-9)^2 + (y+8)^2 = 36}$$

$C(9, -8) \quad r = 6$