

RATIONALS

① $\frac{x+4}{2x+10} \div \frac{x+4}{x+5} = \frac{x+4}{2(x+5)} \cdot \frac{x+5}{x+4} = \boxed{\frac{1}{2}}$

KCF/
FACTOR!

add
nom.

② $\frac{2x+3}{x-2} + \frac{x-4}{x-2} = \boxed{\frac{3x-1}{x-2}}$

③ $\frac{x+1}{(x+5)(x-2)} - \frac{3(x+5)}{(x-2)(x+5)} = \frac{-2(x+7)}{(x+5)(x-2)}$

$\frac{x+1-3x-15}{(x+5)(x-2)} = \boxed{\frac{-2x-14}{(x+5)(x-2)}}$

GRAPH.

Asymptotes? Hole?

$\frac{x+2}{x^2-x-6}$

HA: $y=0$ ← num. < denom.

num. ≠ denom.
no HA

num. = denom.

$y = \frac{2x-3}{3x-4}$

HA: $y = \frac{2}{3}$

FACTOR! $\frac{x+2}{(x+2)(x-3)}$ matching factor → Hole at $x+2=0$
 $(-2, -\frac{1}{5})$

$\frac{1}{x-3}$ VA: $x=3$
 $x-3=0$

CIRCLES

$$(x-3)^2 + (y+5)^2 = 64$$

center $(3, -5)$

radius = $\sqrt{64} = 8$

$$x^2 + y^2 + 4x - 8y = 5$$

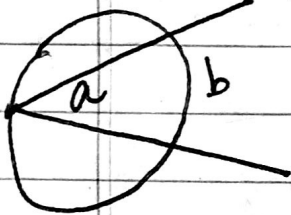
$$(x^2 + 4x + \frac{4}{2}) + (y^2 - 8y + \frac{16}{2}) = 5 + \frac{4}{2} + \frac{16}{2}$$

$$\left(\frac{4}{2}\right)^2 = 4$$

$$\left(\frac{-8}{2}\right)^2$$

$$(x+2)^2 + (y-4)^2 = 25$$

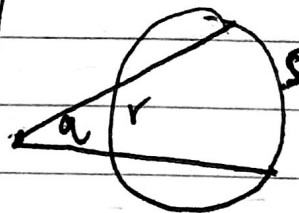
$C(-2, 4) \quad r=5$



Inscribed \neq

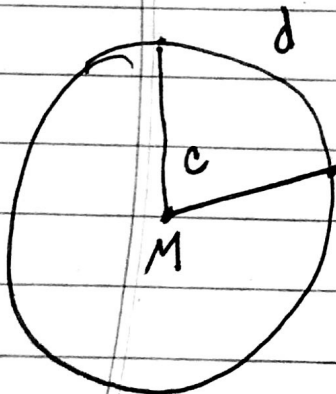
$$2a = b$$

$$a = \frac{1}{2}b$$



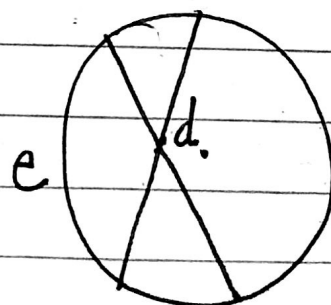
'outsider'

$$a = \frac{1}{2}(s-r)$$



Central \neq

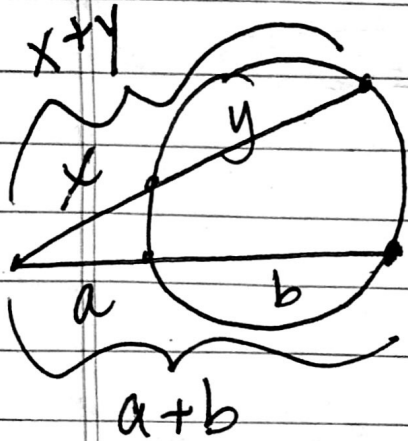
$$c = d$$



'insider'

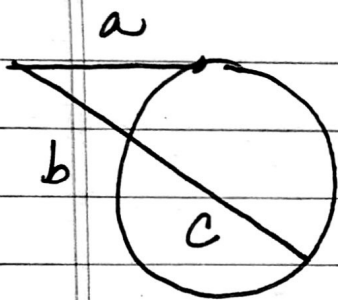
$$d = \frac{1}{2}(e+f)$$

2 secants



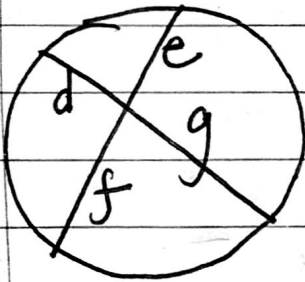
$$W \cdot E = W \cdot E$$

$$(x+y)(x) = (a+b)a$$



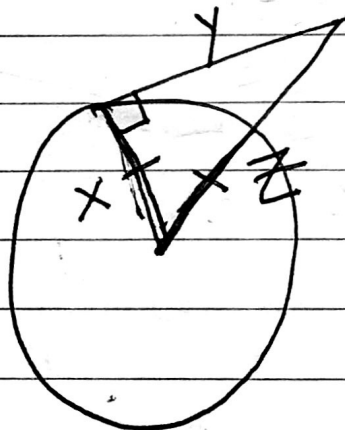
$$W \cdot E = T \cdot T$$

$$(b+c)b = a^2$$



$$P \cdot P = P \cdot P$$

$$e \cdot f = d \cdot g$$



Pythag. Thm.

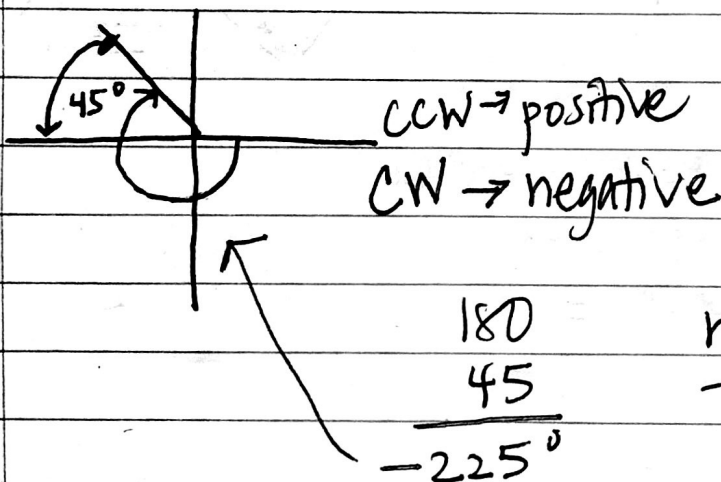
$$x^2 + y^2 = z^2$$

Trig

Unit circle (x, y)
 $(\cos \theta, \sin \theta)$ $\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{y}{x}$

$60^\circ \left(\frac{1}{2}, \frac{\sqrt{3}}{2} \right)$

$\cos 60^\circ = \frac{1}{2}$
 $\sin 60^\circ = \frac{\sqrt{3}}{2}$
 $\tan 60^\circ = \frac{\sqrt{3}}{2} = \frac{\sqrt{3} \cdot \cancel{2}}{\cancel{2} \cdot 1} = \sqrt{3}$



ref $\angle = 45^\circ$
 ACUTE
 positive
 to the x-axis

coterminal
 $\pm 360 / \pm 2\pi$

$$120^\circ \cdot \frac{\pi}{180} = \frac{2\pi}{3}$$

$$\frac{5\pi}{4} \cdot \frac{180}{\pi} = 225^\circ$$

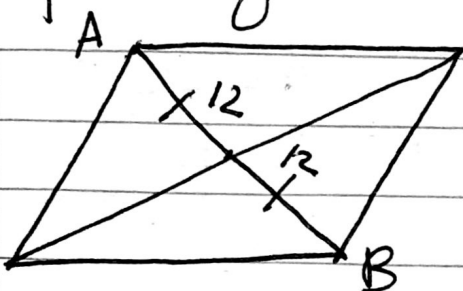
$S = \theta r$
 (arc length) \downarrow in radians

$$A = \frac{1}{2} r^2 \theta$$

QUADS

parallelogram - diagonals NOT congruent

diag. bisect each other

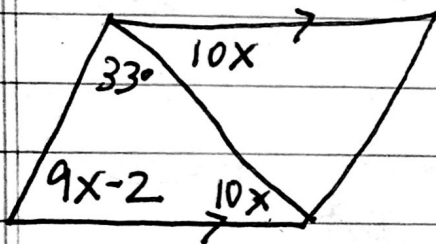


$$AB = 2x - 10$$

$$2x - 10 = 24$$

$$2x = 34$$

$$x = 17$$



Opp. sides \parallel \rightarrow alt. int. \cong

$$9x - 2 + 10x + 33 = 180$$

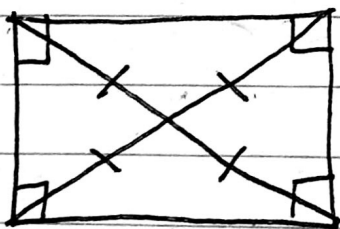
$$19x + 31 = 180$$

$$19x = 149$$

$$x = 7.84$$

Rectangle

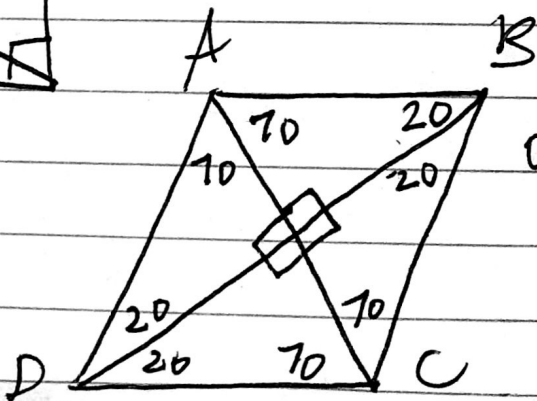
diag. ARE congruent!
all right \angle s



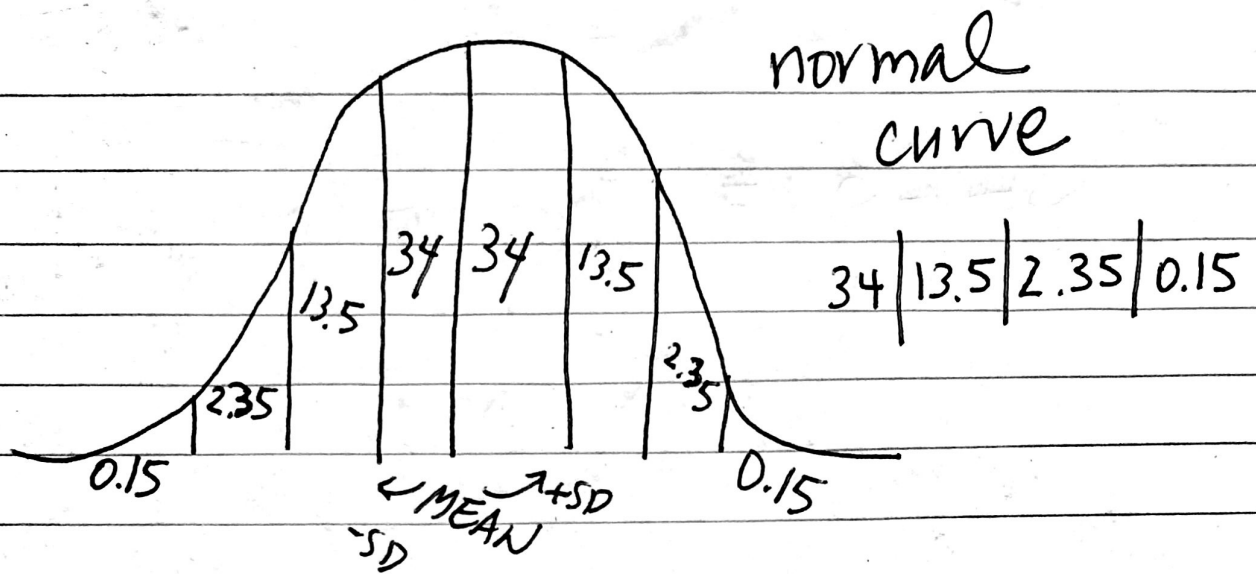
Rhombus

all sides \cong

diag. \perp



Opp. \angle s bisected



Sampling methods

cluster vs. stratified

divided
ALL of
a group

divided
random from
each group

$$y = 3 \sin 4(\theta - 90^\circ) + 2$$

\downarrow amplitude \downarrow $k \rightarrow \frac{360}{k} = \text{period}$

PS VS